

*L3 Mention Informatique
Parcours Informatique et MIAGE*

Génie Logiciel Avancé - Advanced Software Engineering

White-Box Tests (Rev)

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Towards **Static** Program-based Unit Test

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 - ❑ What could be a coverage criterion ?
(or: adequacy criterion,
telling that we "tested enough")

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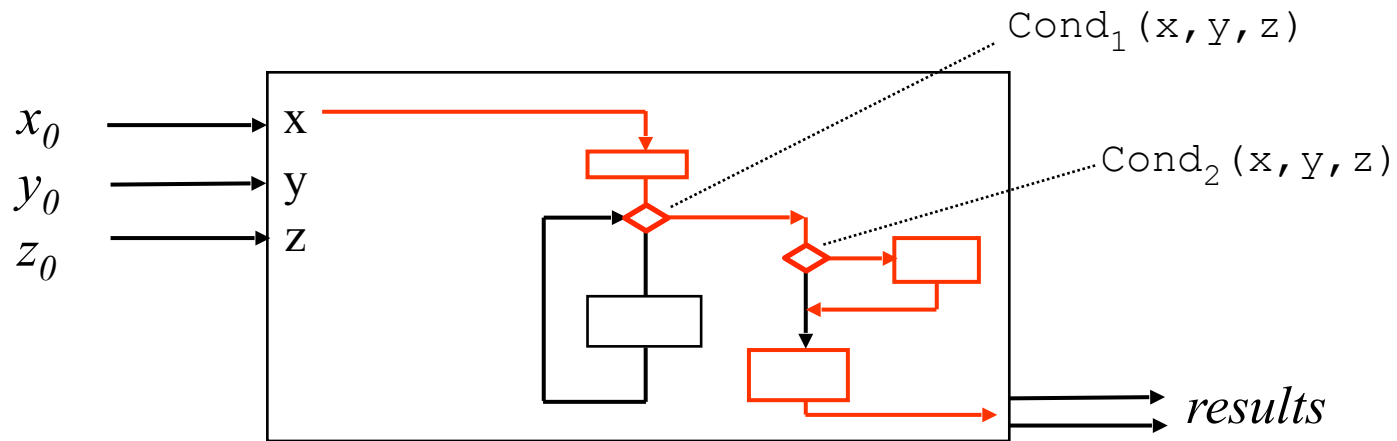
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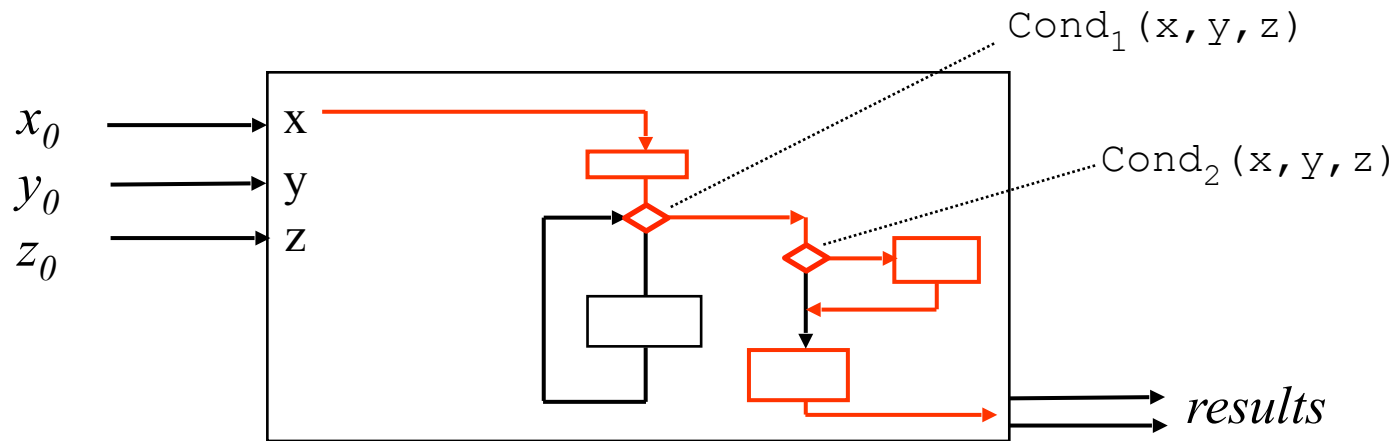
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- ❑ Lets develop a test method that exploits this !

Static Structural ("white-box") Tests

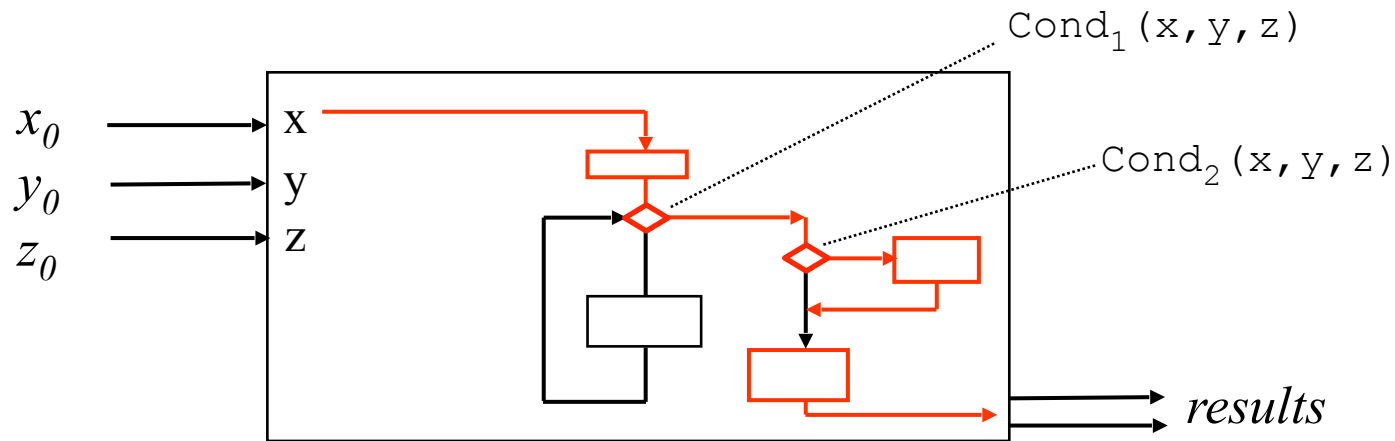


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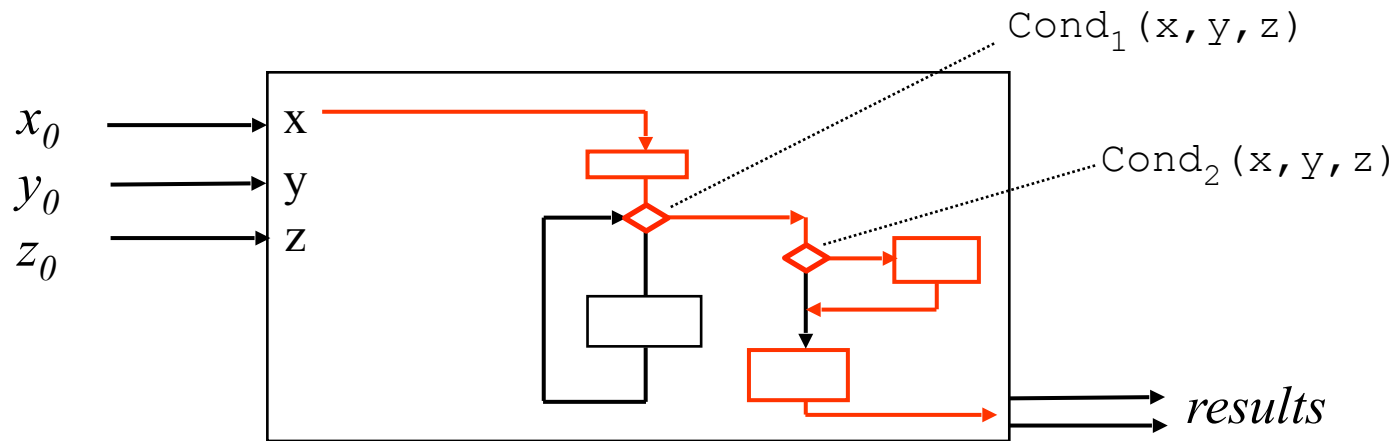
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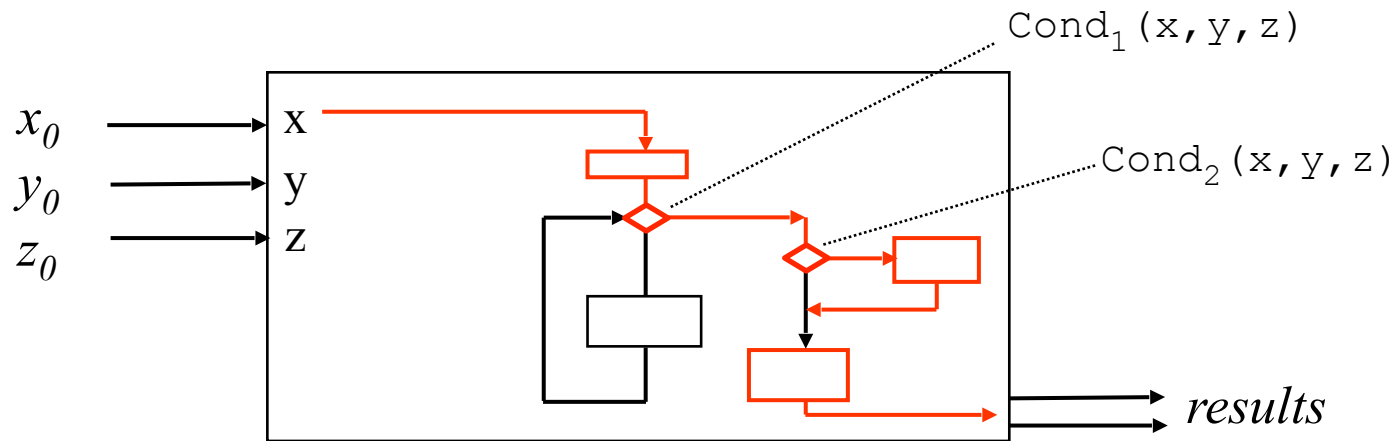


- ❑ we select "critical" paths
- ❑ specification used to verify the obtained resultants

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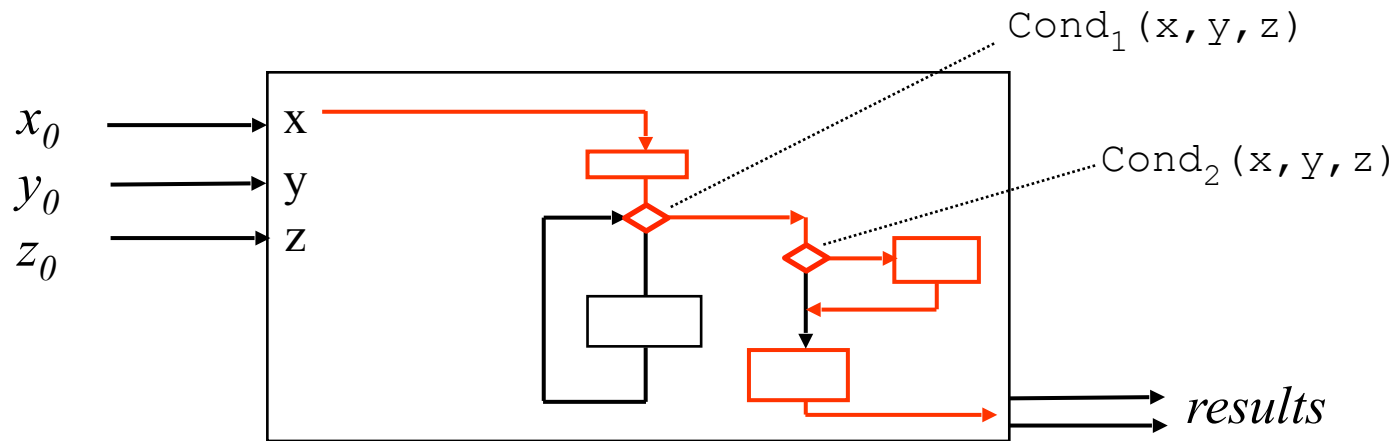
Idea:

*a path corresponds to one logical expression over initial values x_0, y_0, z_0 .
corresponding to one test-case (comprising several test data ...)*

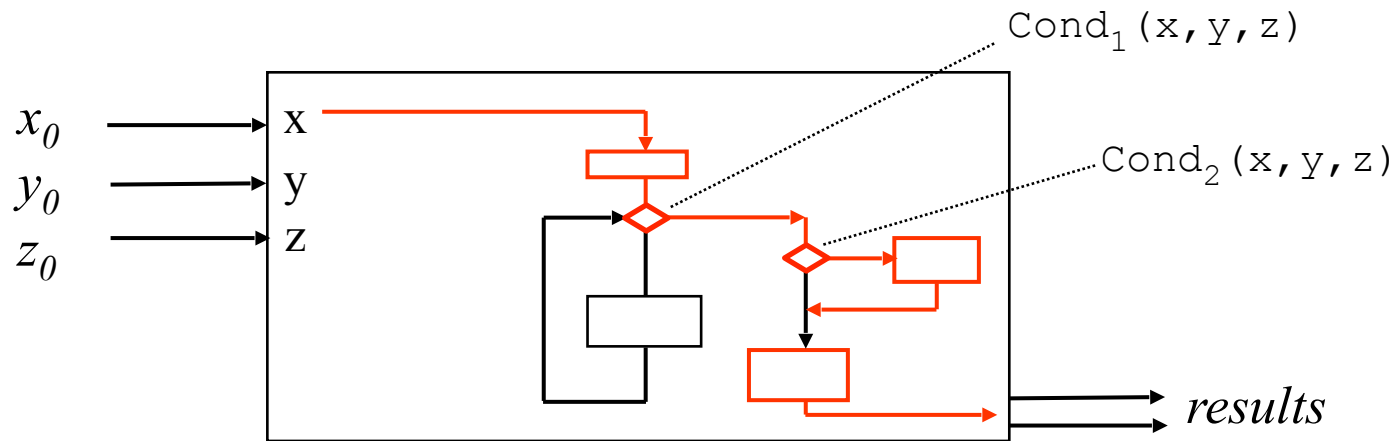
$$\neg Cond_1(x_0, y_0, z_0) \wedge \neg Cond_2(x_0, y_0, z_0)$$

We are interested either in edges (control flow), or in nodes (data flow)

Static Structural ("white-box") Tests



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Recall: This path-condition can be effectively constructed by a process called “symbolic execution”

The notion of a "coverage criterion"

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A coverage criterion is a function mapping a CFG to a particular subset of its paths ...

- the set of paths covering all basic blocks
- the set of paths covering all conditions
- the set with all loops are traversed
- a particular subset of calls/labels occurring in the CFG has been covered
- ...

Well-known Coverage Criteria I

Criterion C = AllInstructions(CFG):

For all nodes N in CFG (basic instructions or decisions)
exists a path in C that contains N

Well-known Coverage Criteria II

Criterion C = AllTransitions(CFG):

For all arcs A in the CFG exists a path in C that uses A

Well-known Coverage Criteria III

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All possible paths ...

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A Hierarchy of Coverage Criteria

- AllPaths(CFG) \supseteq
AllPaths_k(CFG) \supseteq
AllTransitions(CFG) \supseteq
AllInstructions(CFG)
- Each of these implications reflects a proper containment; the other way round is never true.

Schmankerle

□ Program:

```
int f (int a) {  
    int i = 0;  
    int tm = 1;  
    int sum = 1;  
    while(sum <= a) {  
        i = i+1;  
        tm = tm+2;  
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    }  
    return i;  
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Specification:

```
pre :  $a \geq 0$   
post:  $a \leq \text{result}^2 \wedge a < (\text{result}+1)^2$ 
```

Schmankerle

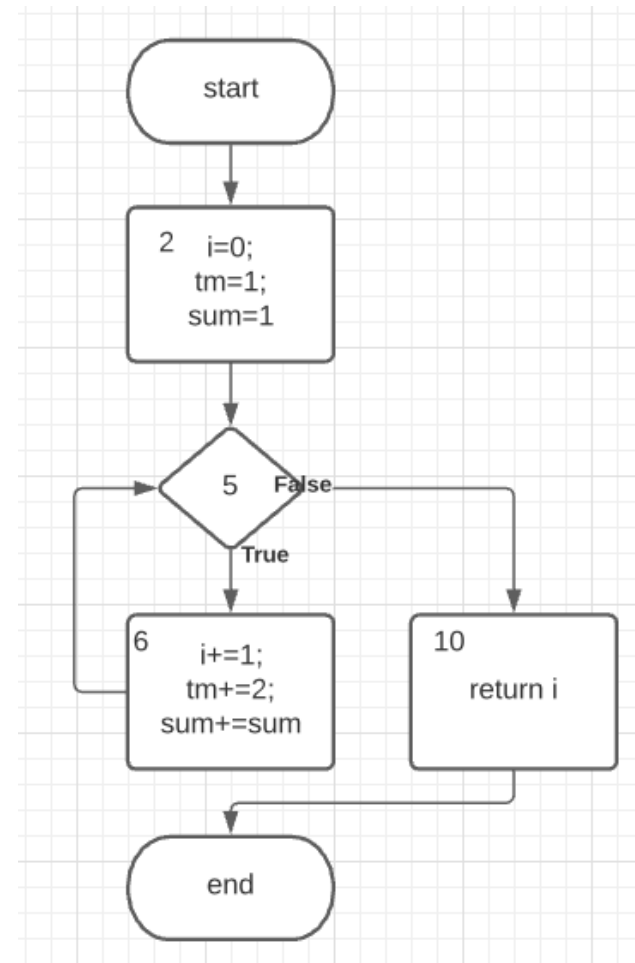
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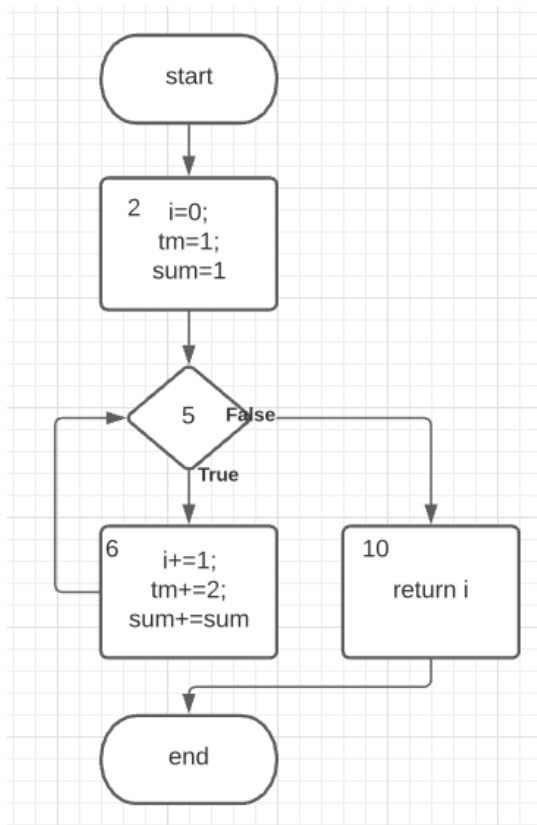


Schmankerle

▣ CFG de f:

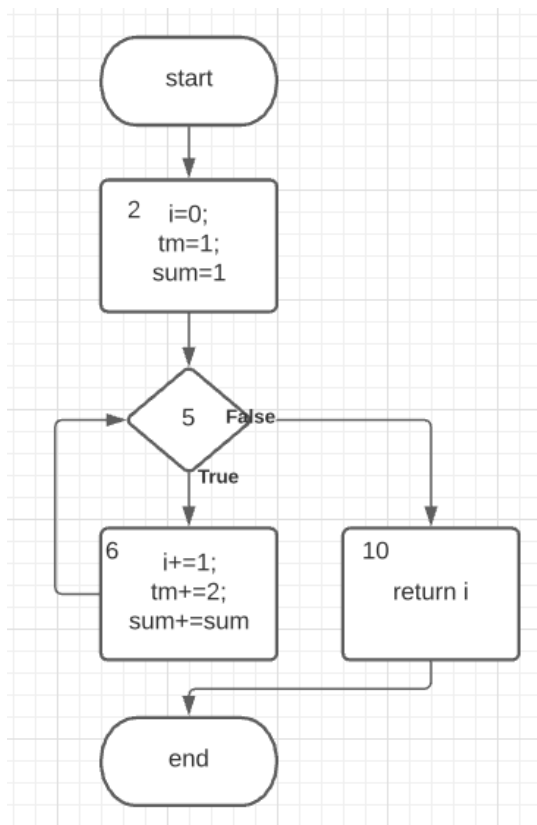
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CFG de f:



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CFG de f:



For example:

AllInstructions(CFG)={ [start,2,5,6,5,10,end] }

AllTransitions(CFG)={ [start,2,5,6,5,10,end] }

AllPath₃(CFG)={ [start,2,5,10,end],
[start,2,5,6,5,10,end],
[start,2,5,6,6,5,10,end],
[start,2,5,6,6,6,5,10,end] }

AllPath(CFG)={ S | $\exists k \in \mathbb{N}$.

S = [start,2,5,(6,5)^k,10,end] }
(infinite !)

Example: A Symbolic Path Execution

We want to execute the path from AllPath₃:

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Example: A Symbolic Path Execution

Result:

Test-Case:

For the path $M=[\text{start},2,5,6,5,10,\text{end}]$

we have the path condition $\Phi \mapsto 1 \leq a_0 \wedge 4 > a_0$

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